Search for 2β decay of cadmium and tungsten isotopes: Final results of the Solotvina experiment

F. A. Danevich, A. Sh. Georgadze, V. V. Kobychev, B. N. Kropivyansky, A. S. Nikolaiko, O. A. Ponkratenko, V. I. Tretyak,

S. Yu. Zdesenko, and Yu. G. Zdesenko*

Institute for Nuclear Research, MSP 03680 Kiev, Ukraine

P. G. Bizzeti, T. F. Fazzini, and P. R. Maurenzig Dipartimento di Fisica, Universitá di Firenze and INFN, 50019 Firenze, Italy (Received 21 March 2003; published 4 September 2003)

Final results of the double β decay experiment, performed with the help of low background ¹¹⁶CdWO₄ crystal scintillators in the Solotvina Underground Laboratory, are presented. In particular, the revised half-life value of the two-neutrino 2β decay of ¹¹⁶Cd has been measured as $T_{1/2}^{2\nu} = 2.9_{-0.3}^{+0.4} \times 10^{19}$ yr, and the new half-life limit on the neutrinoless 2β decay of ¹¹⁶Cd has been established as $T_{1/2}^{0\nu} \ge 1.7(2.6) \times 10^{23}$ yr at 90% (68%) C.L. The latter corresponds to a restriction on the neutrino mass: $m_{\nu} \le 1.7(1.4)$ eV at 90% (68%) C.L. Besides, new $T_{1/2}$ bounds (at the level of $10^{17} - 10^{21}$ yr) were set for various 2β processes in ¹⁰⁶Cd, ¹⁰⁸Cd, ¹¹⁴Cd, ¹⁸⁰W, and ¹⁸⁶W nuclei.

DOI: 10.1103/PhysRevC.68.035501

PACS number(s): 23.40.-s, 27.60.+j, 27.70.+q, 29.40.Mc

I. INTRODUCTION

Recent observations of neutrino oscillations [1-4] provide important motivation for double beta (2β) decay experiments [5–7]. Indeed, the neutrinoless (0ν) mode of 2β decay, which violates lepton number (L) conservation and requires the neutrino to be a massive Majorana particle, is forbidden in the framework of the standard model (SM) of electroweak theory. However, many extensions of the SM incorporate L violating interactions and, thus, could lead to this process, which, when observed, would prove the Majorana nature of the neutrino. Hence, the discovery of the $0\nu 2\beta$ decay would be a clear evidence for a new physics beyond the SM [5-7]. Moreover, while oscillation experiments are sensitive to the neutrino mass difference, the measured $0\nu 2\beta$ decay rate can give the absolute scale of the effective Majorana neutrino mass and test different neutrino mixing models.

Despite numerous experimental efforts this process still remains unobserved, and only half-life limits for 0ν mode have been obtained in direct experiments up to now (see reviews in Refs. [5–8]). The highest bounds have been established for several nuclides: $T_{1/2}^{0\nu} \ge 10^{21}$ yr for ⁴⁸Ca [9], ¹⁵⁰Nd [10], ¹⁶⁰Gd [11], ¹⁸⁶W [12]; $T_{1/2}^{0\nu} \ge 10^{22}$ yr for ⁸²Se [13], ¹⁰⁰Mo [14]; $T_{1/2}^{0\nu} \ge 10^{23}$ yr for ¹¹⁶Cd [15], ¹²⁸Te, ¹³⁰Te [16], ¹³⁶Xe [17]; and $T_{1/2}^{0\nu} \ge 10^{25}$ yr for ⁷⁶Ge [18,19].

In the present paper we describe the final results of the ¹¹⁶Cd 2β decay studies, which have been performed by using cadmium tungstate crystal scintillators (with natural isotopic composition crystals and ones enriched in ¹¹⁶Cd to 83%) in the Solotvina Underground Laboratory [20] since 1988 [21]. The results obtained on the different phases of these researches have been published earlier [21–28,15,29,12]. The Solotvina experiment has been stopped in July 2002.

*Corresponding author. Email address: zdesenko@kinr.kiev.ua

II. EXPERIMENT AND DATA ANALYSIS

A. The low background setup

Description of the last modification of the setup with cadmium tungstate (CdWO₄) crystal scintillators and its performance have been already published [15], thus only the main features of this apparatus are summarized here. The experiment was carried out in the Solotvina Underground Laboratory at a depth of 1000 m of water equivalent [20]. The ¹¹⁶CdWO₄ crystal scintillators, enriched in ¹¹⁶Cd to 83%, have been grown for the search [21]. Their light output is $\approx 30-35\%$ as compared with that of NaI(Tl). The fluorescence peak emission is at 480 nm with principal decay time of $\approx 13 \ \mu$ s. Four ¹¹⁶CdWO₄ crystals with a total mass of 330 g were used in the setup. These are viewed by a low background 5" EMI D724KFL photomultiplier (PMT) through one light guide 10 cm in diameter and 55 cm long. The light guide consists of two parts: high purity quartz (25 cm) and plastic scintillator (30 cm). The $^{116}CdWO_4$ crystals are surrounded by an active shield made of 15 CdWO₄ crystals of large volume with a total mass of 20.6 kg [30,31]. These are viewed by a low background PMT through an active plastic light guide 17 cm in diameter and 49 cm long. The whole $CdWO_4$ array is situated within an additional active shield made of plastic scintillator $40 \times 40 \times 95$ cm, thus, together with both active light guides, a complete 4π active shield of the main (¹¹⁶CdWO₄) detector is provided. The outer passive shield consists of high purity copper (3-6 cm), lead (22.5-30 cm), and polyethylene (16 cm). Two plastic scintillators $(120 \times 130 \times 3 \text{ cm})$ installed above the passive shield serve as cosmic muon veto.

The event-by-event data acquisition is based on two personal computers (PC) and a CAMAC crate with electronic units. For each event within the ¹¹⁶ CdWO₄ detector array, the following information is stored on the hard disk of the first PC: the amplitude of a signal (in the energy range of 0.12-5.4 MeV), its arrival time, and additional tags [the coincidence between the main and shielding detectors; triggers for a light emitting diode (LED) and for the transient digitizer]. The second PC records the pulse shape (2048 channels, each of 50 ns width) of the ¹¹⁶CdWO₄ signals in the energy range 0.3-5.4 MeV (in special runs, the threshold was set at 80 keV) by using the transient digitizer (based on a 12-bit analog-to-digital converter Analog Devices AD9022) connected to the PC by a parallel digital board [32].

The energy scale and resolution of the ¹¹⁶CdWO₄ spectrometer were determined with various γ sources (²²Na, ⁴⁰K, ⁶⁰Co, ¹³⁷Cs, ²⁰⁷Bi, ²²⁶Ra, ²³²Th, and ²⁴¹Am). The energy dependence of the resolution in the energy interval 60–2615 keV is expressed as follows: FWHM_{γ} = -44 $+\sqrt{2800+23.4E_{\gamma}}$, where energy E_{γ} and FWHM are in keV. For instance, energy resolutions of 33.7%, 13.5%, 11.5%, and 8.0% were measured for γ lines with energies of 60, 662, 1064, and 2615 keV, respectively. Routine calibrations were carried out with 207 Bi and 232 Th γ sources. The stability of the spectrometer is demonstrated by the fact that resolution of the ¹³⁷Cs peak in the background spectra (collected over 13 316 hours) is FWHM $\approx 14\%$, which is practically the same as measured in the calibration runs. The dead time of the detector and data acquisition was permanently controlled with the help of a light emitting diode optically connected to the main PMT (typical value was about 4%).

Besides, the relative light yield for α particles as compared with that for β particles (γ rays) with the same energies (so-called α/β ratio, which can be defined as the ratio of the energy of α particles measured in the γ scale of the detector, E_{α}^{γ} , to their actual energy, E_{α}) was determined in the energy range of 2.1-8.8 MeV. First, a collimated beam of α particles from ²⁴¹Am source penetrated through the thin absorbers with known thicknesses was used. The energy of the α particles after the absorber was accurately calculated and was also measured by a surface-barrier detector (we refer for details to work [33]). Second, the α peaks from the intrinsic trace contamination of the ¹¹⁶CdWO₄ crystals by nuclides of the Th chain (selected by the time-amplitude and the pulse-shape analysis as described below) were also utilized for the α/β ratio determination. In addition, we found the dependence of the α/β ratio (and pulse shape as well) on the direction of α particles beam relative to the main crystal axes [33]. Finally, it yields $\alpha/\beta = 0.083(9) + 1.68(13)$ $\times 10^{-5} E_{\alpha}$, and FWHM^{γ}_{α}(keV) = 33 + 0.247 E_{α}^{γ} , where E_{α} and E^{γ}_{α} are in keV.

Due to the active and passive shields, and as a result of the time-amplitude and the pulse-shape analysis of the data (see below), the background rate of the ¹¹⁶CdWO₄ detector in the energy region 2.5–3.2 MeV ($0\nu 2\beta$ decay energy of ¹¹⁶Cd is 2.8 MeV) is reduced to 0.04 counts/(yr kg keV). It is the lowest background rate which has ever been reached with crystal scintillators.

B. Pulse-shape discrimination technique

According to the measured α/β ratio, α particles from uranium and thorium trace contamination of the crystals can produce a background in the 0.4–1.3 MeV energy region, while overlapping of the β and α signals from two fast se-

quential decays, e.g., ²¹²Bi (Q_{β} =2.25 MeV) \rightarrow ²¹²Po (Q_{α} = 8.95 MeV, $T_{1/2}$ =0.3 μ s) \rightarrow ²⁰⁸Pb, would result in a single event with the total energy up to 4.5 MeV. To suppress such a background, a method of pulse-shape analysis (PSA) of CdWO₄ scintillation signals, based on the optimal digital filter [34], was developed [32] and a clear discrimination between γ rays (electrons) and α particles was achieved [32,15,33].

The pulse shape of cadmium tungstate scintillation signal can be described as: $f(t) = \sum A_i / (\tau_i - \tau_0) (e^{-t/\tau_i} - e^{-t/\tau_0}),$ where A_i are amplitudes and τ_i are decay constants for different light emission components, and τ_0 is the integration constant of electronics ($\approx 0.18 \ \mu s$). To provide an analytic description of the α or γ signals, the pulse shape resulting from the average of a large number of individual events has been fitted with the sum of three (for α particles) or two (for γ -s) exponential functions, providing the reference pulse shapes $\overline{f}_{\alpha}(t)$ and $\overline{f}_{\gamma}(t)$. Comparing two independent calibration measurements with the enriched ${}^{116}CdWO_4$ crystals (used in the experiment) the following values for the parameters of γ and α pulse shape were obtained: A_1^{α} = 80.9(1.9)%, τ_1^{α} = 12.7(0.6) μ s, and A_2^{α} = 13.4(1.3)%, τ_2^{α} =3.3(1.1) μ s, A_3^{α} =5.7(1.0)%, τ_3^{α} =0.96(0.08) μ s for \approx 5-MeV α particles, and $A_1^{\gamma} = 94.3(0.3)\%$, τ_1^{γ} =13.6(0.2) μ s and A_2^{γ} =5.7(0.2)%, τ_2^{γ} =2.1(0.1) μ s for \approx 1-MeV γ quanta.

In data processing the digital filter was applied to each experimental signal f(t) with the aim to obtain the numerical characteristic of its shape (shape indicator, SI) defined as SI $=\Sigma f(t_k)P(t_k)/\Sigma f(t_k)$, where the sum is over time channels k, starting from the onset of signal and up to 75 μ s, $f(t_k)$ is the digitized amplitude (at the time t_k) of a given signal. The weight function P(t) is defined as $P(t) = \{\overline{f}_{\alpha}(t) - \overline{f}_{\gamma}(t)\}/\{\overline{f}_{\alpha}(t) + \overline{f}_{\gamma}(t)\}$.

The SI distributions measured with different α and γ sources (some examples are shown in Fig. 1) are well described by Gaussian functions, whose standard deviations $\sigma(SI_{\alpha})$ and $\sigma(SI_{\gamma})$ depend on energy [32,33]. As it is seen from Fig. 1, electrons (γ rays) and α particles are clearly distinguished for the energies above 0.8 MeV ($E_{\alpha} \approx 3.8$ MeV). Although the pulse-shape discrimination ability worsens at lower energies, even 2-MeV α particles ($E_{\alpha}^{\gamma} \approx 0.3$ MeV) can be separated from γ background with reasonable accuracy [33]. An illustration of the PSA of the background events (for energy above 350 keV) is presented in Fig. 2 as three-dimensional distribution of the background events, which belong to U/Th families, and $\gamma(\beta)$ events.

In conclusion, the PSA allows us to reject α decays and other background events such as double pulses, the plastic light guide signal overlapping, noise, etc. For example, the α peak of ²¹²Po (the daughter of the ²¹²Bi) was reconstructed with the help of the front edge analysis of the scintillation signals. The energy and time distributions of the sequence of β decay of ²¹²Bi and α decay of ²¹²Po, selected from the background, are presented in Figs. 3(a–c), while a typical example of such an event is shown in Fig. 3(d). Similarly, the



FIG. 1. Examples of the shape indicator distributions for the α particles and γ rays measured by the enriched ¹¹⁶CdWO₄ crystal scintillator (32×19 mm): (a) E_{γ} =0.8–1.0 MeV, E_{α} =3.88 MeV; (b) E_{γ} =1.2–1.4 MeV, E_{α} =5.25 MeV. The crystal was irradiated by α particles in a direction perpendicular to the (010) crystal plane [33].

events from the ${}^{214}\text{Bi} \rightarrow {}^{214}\text{Po} \rightarrow {}^{210}\text{Pb}$ chain were recognized, too. As a result, the events caused by two fast decays in both chains $({}^{212}\text{Bi} \rightarrow {}^{212}\text{Po} \rightarrow {}^{208}\text{Pb}$ and ${}^{214}\text{Bi} \rightarrow {}^{214}\text{Po} \rightarrow {}^{210}\text{Pb})$, which can result in background events with energies up to 4.5 MeV, were discarded from the data.



FIG. 2. Three-dimensional distribution of the background events (2975 h of exposition with the ¹¹⁶CdWO₄ crystals) versus energy and shape indicator. The population of α events belonging to the U/Th families is clearly separated from the population of $\gamma(\beta)$ events.



FIG. 3. (Color online) The energy (a,b) and time (c) distributions for the fast sequence of β (²¹²Bi, $Q_{\beta}=2254$ keV) and α [²¹²Po, $E_{\alpha}=8785$ keV, $T_{1/2}=0.299(2)$ μ s] decays selected from the background data by the pulse-shape analysis. (d) Example of such an event in the ¹¹⁶CdWO₄ scintillator.

C. Time-amplitude analysis of the data

The energy and the arrival time of each event were used for analysis and selection of some decay chains in ²³²Th, ²³⁵U, and ²³⁸U families. For instance, the following sequence of α decays from the ²³²Th family was searched for and observed: 224 Ra $(Q_{\alpha} = 5.79 \text{ MeV}) \rightarrow {}^{220}$ Rn $(Q_{\alpha} = 6.40 \text{ MeV}, {}_{71/2} = 55.6 \text{ s}) \rightarrow {}^{216}$ Po $(Q_{\alpha} = 6.91 \text{ MeV}, {}_{71/2} = 5.6 \text{ s})$ =0.145 s) \rightarrow^{212} Pb. Because the energy of α particles from ²²⁰Rn decay corresponds to $\simeq 1.2$ MeV in the γ scale of the ¹¹⁶CdWO₄ detector, the events in the energy region 0.6-2.0MeV were used as triggers. Then, all events (within 0.6-2.0 MeV) following the triggers in the time interval 10-1000 ms (containing 95% of ²¹⁶Po decays) were selected. Then in the next step of the analysis, the fast couples found (²²⁰Rn and ²¹⁶Po) were used as triggers to search for preceding α decays of ²²⁴Ra. The time window was set as 1-111 s (it contains 74% of ²²⁰Rn decays). The obtained α peaks (the α nature of events was confirmed by the pulse-shape analysis described above), as well as the distributions of the time intervals between events are in a good agreement with those expected for α particles of ²²⁴Ra, ²²⁰Rn, and ²¹⁶Po (see Fig. 4). On this basis the activity of 228 Th in the 116 CdWO₄ crystals was determined as 39(2) μ Bq/kg. By analyzing the behavior of the 228 Th activity within the time interval 5–13 yr after the growth of crystals we have estimated the ²³²Th activity in the ¹¹⁶CdWO₄ scintillators as 53(9) μ Bq/kg, and a limit for the ²²⁸Ra activity $\leq 4 \mu Bq/kg$.

The same technique was applied to the sequence of α decays from the ²³⁵U family: ²²³Ra (Q_{α} =5.98 MeV) \rightarrow ²¹⁹Rn (Q_{α} =6.95 MeV, $T_{1/2}$ =3.96 s) \rightarrow ²¹⁵Po (Q_{α} =7.53 MeV, $T_{1/2}$ =1.78 ms) \rightarrow ²¹¹Pb. For the first couple



FIG. 4. The α peaks of ²²⁴Ra, ²²⁰Rn, and ²¹⁶Po selected by the time-amplitude analysis from the data accumulated during 14 745 h with the ¹¹⁶CdWO₄ detector. In the insets the time distributions between the first and second (and between second and third) events together with exponential fits are presented. Obtained half-lives of ²²⁰Rn and ²¹⁶Po $[61^{+10}_{-8}$ s and 0.144(8) s, respectively] are in a good agreement with the table values: 55.6(1) s and 0.145(2) s [36].

 $(^{219}\text{Rn} \rightarrow ^{215}\text{Po})$ all events within 0.6–2.2 MeV were used as triggers, while a time interval 1–10 ms (66% of ^{215}Po decays) and an energy window 0.6–2.2 MeV were set for the second events. The obtained α peaks correspond to an activity of 1.4(9) μ Bq/kg for the 227 Ac impurity in the crystals.

As regards the ²²⁶Ra chain (²³⁸U family), the following sequence of β and α decays was analyzed: ²¹⁴Bi ($Q_{\beta} = 3.27 \text{ MeV}$) \rightarrow ²¹⁴Po ($Q_{\alpha} = 7.83 \text{ MeV}$, $T_{1/2} = 164.3 \mu s$) \rightarrow ²¹⁰Pb. The obtained results give for the activity of ²²⁶Ra in the ¹¹⁶CdWO₄ crystals a limit $\leq 4 \mu Bq/kg$.

Finally, all correlated events found for ²³²Th, ²³⁵U, and ²³⁸U families were eliminated from the measured data, while information about measured intrinsic activities of the crystals was used for the background reconstruction in the procedure of data analysis.

III. MEASUREMENTS AND RESULTS

A. Background interpretation

The energy spectrum of the $\gamma(\beta)$ events measured during 13 316 h of the live time in the low background setup with the ¹¹⁶CdWO₄ crystal scintillators (and selected by the PSA) is shown in Fig. 5. In the low energy region the background is caused mainly by the fourth-forbidden β decay of ¹¹³Cd ($T_{1/2}$ =7.7×10¹⁵ yr [35], Q_{β} = 316 keV [36]) and β decay of ^{113m}Cd ($T_{1/2}$ =14.1 yr, Q_{β} =580 keV [36]).¹ The distribution above ≈0.5 MeV is described by the 2 $\nu 2\beta$ decay spec-



FIG. 5. (Color online) Spectrum of $\gamma(\beta)$ events measured with ¹¹⁶CdWO₄ detectors during 13 316 h and selected by the pulseshape analysis. Solid line represents the fit of the data by the background model in the 340–2700-keV-energy interval. Also shown are the most important components of the background: β spectra of ¹¹³Cd and ^{113m}Cd, $2\nu 2\beta$ spectrum of ¹¹⁶Cd with $T_{1/2}^{2\nu}=2.9$ $\times 10^{19}$ yr, and model distribution of external γ -s.

trum of ¹¹⁶Cd with $T_{1/2}^{2\nu} = 2.9 \times 10^{19}$ yr (see below), trace contamination of the enriched and shield crystals by ¹³⁷Cs and 40 K, and external γ rays. The energy distributions for the above mentioned background components were simulated with the help of the code GEANT3.21 [37] and the event generator DECAY4 [38].² The least squares fit ($\chi^2/ndf = 119/108$ =1.1) of the experimental spectrum in the 0.34--2.7 MeV energy interval by the sum of the components listed above (to describe external γ -s an exponential function was used in addition to the ⁴⁰K, ²³²Th, and ²³⁸U contamination of the PMTs, whose activities were previously measured [27]) gives the following intrinsic activities of the ¹¹⁶CdWO₄ crystals (in mBq/kg): 1.1(1) for ^{113m}Cd, 0.43(6) for ¹³⁷Cs, and 0.3(1) for ⁴⁰K. The ⁴⁰K contamination of the shielding CdWO₄ crystals was calculated to be 1.5(3) mBq/ kg. The fitting curve and main components of the background are presented in Fig. 5.

In addition, the fit was repeated with the described model, into which other impurities were included: 210 Pb, 234m Pa (238 U family), 228 Ac (232 Th), and 90 Sr (in equilibrium with

¹The abundance of ¹¹³Cd in the enriched crystals was measured with the help of mass spectrometer as $\delta = 2.15(20)\%$ [25]. The possible presence of ^{113m}Cd in the CdWO₄ scintillators was confirmed by the low background measurements with two crystals,

where the β spectrum of ^{113m}Cd was observed [30].

²The accuracy of the Monte Carlo simulation was checked in the series of the dedicated measurements with the calibration radioactive sources (γ -²²Na, ⁵⁴Mn, ⁶⁰Co, ¹³⁷Cs, ²⁰⁷Bi, ²³²Th; β -⁹⁰Sr, ²¹⁰Bi), and with several cadmium tungstate crystals of different sizes. The various detector assemblies were used, beginning from a simplest "detector plus source" design, and ending with the actual low background setup, which includes the anticoincidence scintillators. The measured spectra were simulated with the help of GEANT3.21 and DECAY4 codes as described above. A good agreement between the simulated and experimental results was obtained for each detector configuration, which allows us to use the Monte Carlo simulation for the background reconstruction, and to build up models of the different 2 β processes searched for [39].



FIG. 6. (Color online) Low energy part of the spectrum measured during 692 h by the ¹¹⁶CdWO₄ detectors with an energy threshold of 80 keV [the $\gamma(\beta)$ events were selected by the PSA with efficiency of 98%]. The fitting curve is drawn by the solid line. Shadowed distribution is $2\nu 2\beta$ decay spectrum of ¹⁸⁶W with $T_{1/2}^{2\nu}$ = 3.7×10^{18} yr excluded at 90% C.L. Inset: The part of the spectrum together with the $2\nu 2K$ peak of ¹⁸⁰W with $T_{1/2}^{2\nu 2K} = 0.7 \times 10^{17}$ yr (dotted line) and $0\nu 2\varepsilon$ peak of ¹⁸⁰W with $T_{1/2}^{0\nu 2\varepsilon} = 0.9 \times 10^{17}$ yr (shadowed), both excluded at 90% C.L.

⁹⁰Y). However, only limits on their activities in the ¹¹⁶CdWO₄ scintillators were obtained, as follows (mBq/kg): ²¹⁰Pb \leq 0.4, ^{234m}Pa \leq 0.2, ²²⁸Ac (²²⁸Ra) \leq 0.1, and ⁹⁰Sr \leq 0.2.

The lowest energy part of the experimental spectrum is dominated by the β spectrum of ¹¹³Cd (see Fig. 6). To determine its activity, the background of the ¹¹⁶CdWO₄ detectors was measured during 692 h with the energy threshold of 80 keV, which allows us to extend the PSA technique to this energy region. Fitting the data by a sum of the simulated β spectrum of ¹¹³Cd and an exponential function (to describe residual background) we estimate the activity of ¹¹³Cd in the enriched crystals as 91(5) mBq/kg. It corresponds to an abundance of this isotope in the ¹¹⁶CdWO₄ crystals δ = 1.9(2)%, which is in agreement with the result of mass-spectrometric measurement δ =2.15(20)% [25].

All data on radioactive contamination of the ¹¹⁶CdWO₄ crystal scintillators are summarized in Table I.

B. Two-neutrino double β decay of ¹¹⁶Cd

The level scheme of the ¹¹⁶Cd-¹¹⁶In-¹¹⁶Sn triplet [36] is depicted in Fig. 7(a), while the response functions of the ¹¹⁶CdWO₄ detector for the different channels of the $2\nu 2\beta$ and $0\nu 2\beta$ decay of ¹¹⁶Cd (simulated with the help of GEANT3.21 and DECAY4 codes) are shown in Figs. 7(b) (g.s. \rightarrow g.s. transitions, where g.s. corresponds to ground state) and 8 (transitions to excited levels of ¹¹⁶Sn).

Earlier, after 4629 h of data accumulation in our experiment, the preliminary half-life value of two-neutrino 2β decay of ¹¹⁶Cd was reported as $T_{1/2}^{2\nu} = 2.6 \pm 0.1(\text{stat})_{-0.4}^{+0.7}(\text{syst})$ $\times 10^{19}$ yr [15]. In the present work, with the aim to derive a refined $T_{1/2}^{2\nu}$ value, we are using the advantage of higher statistics (12 649 h) collected after the last upgrade of the setup

TABLE I. Activities of different nuclides present in the 116 CdWO₄ crystal scintillators.

Chain	Nuclide	Activity (mBq/kg)
²³² Th	²³² Th	0.053(9)
	²²⁸ Ra	≤0.004
	²²⁸ Th	0.039(2)
²³⁸ U	$^{238}\text{U} + ^{234}\text{U}$	≤0.6
	^{234m} Pa	≤0.2
	²³⁰ Th	≤0.5
	²²⁶ Ra	≤0.004
	²¹⁰ Pb	≤0.4
²³⁵ U	²²⁷ Ac	0.0014(9)
	40 K	0.3(1)
	⁹⁰ Sr	≤0.2
	¹¹³ Cd	91(5)
	113m Cd	1.1(1)
	¹³⁷ Cs	0.43(6)

in 1999 when spectrometric parameters of the detector (in particular, the energy resolution and pulse shape discrimination ability) were improved. The ¹¹⁶CdWO₄ crystals contain 4.54×10^{23} nuclei of ¹¹⁶Cd, therefore the exposure of the experiment is 6.56×10^{23} nuclei × yr. The total efficiency for detecting the $2\nu 2\beta$ decay of ¹¹⁶Cd by the ¹¹⁶CdWO₄ crys-



FIG. 7. (a) (Color online) The level scheme of the ¹¹⁶Cd-¹¹⁶-In-¹¹⁶Sn triplet. The $Q_{\beta\beta}$ energy is taken from [40]. (b) Simulated response functions of the ¹¹⁶CdWO₄ crystal scintillators for the 2ν and 0ν modes of the 2β decay of ¹¹⁶Cd to the ground level of ¹¹⁶Sn.

Origin of the systematic error	Range	Contribution to $T_{1/2}^{2\nu}$ value, 10^{19} yr
Live measuring time	(96±2)%	±0.06
Efficiency of the PS analysis	97^{+1}_{-3} %	+0.03, -0.09
Detection efficiency of the $2\nu 2\beta$ decay	(96±3)%	± 0.09
(GEANT model uncertainty)		
Fit in different energy regions		+0.2, -0.3
$^{90}\mathrm{Sr}-^{90}\mathrm{Y}$ and $^{234m}\mathrm{Pa}$ impurity in $^{116}\mathrm{CdWO}_4$	$\leq 0.3 \text{ mBq/kg}$	+0.35

TABLE II. Different origins of the systematical uncertainties and their contributions to the half-life value of ¹¹⁶Cd two-neutrino 2β decay.

tals is calculated as 0.93 (Monte Carlo simulation gives the registration efficiency of the $2\nu 2\beta$ decay events as $\eta_{mc} = 0.96$, while the efficiency of the PSA selection of $\gamma(\beta)$ events is $\eta_{psa} = 0.97$).

The part of the experimental spectrum used for the data analysis is depicted in Fig. 9. The data in the energy interval 800–2800 keV were simulated with the help of the GEANT3.21 package and the event generator DECAY4. In addition to the ¹¹⁶Cd two-neutrino 2β decay distribution, only three background components were considered. These are ⁴⁰K contamination of the enriched and nonenriched CdWO₄ scintillators, and external γ background caused by ⁴⁰K, ²³²Th, and ²³⁸U contamination of the PMTs. The radioactive impurities of each PMT were previously measured as (2–4) Bq/PMT for ⁴⁰K, and (0.4–2.2) and (0.1–0.2) Bq/PMT for ²²⁶Ra and ²²⁸Th activity, respectively [27].

The fit of experimental data in the energy interval 860–2700 keV (χ^2 /ndf=64/86=0.7) gives the following results: the activities of ⁴⁰K inside the enriched and nonenriched CdWO₄ crystals are equal to 0.4(2) and 1.6(4) mBq/kg, respectively; the half-life value of the $2\nu 2\beta$ decay of ¹¹⁶Cd is $2.93\pm0.06(\text{stat})\times10^{19}$ yr (the corresponding activity in the enriched crystals is about 1 mBq/kg).³

The quality of our results can be judged on the basis of the deduced $2\nu 2\beta$ Kurie plot: $K(\varepsilon) = [S(\varepsilon)/\{(\varepsilon^4 + 10\varepsilon^3 + 40\varepsilon^2 + 60\varepsilon + 30)\varepsilon\}]^{1/5}$, where *S* is the number of events with energy ε (in units of electron mass) in the experimental spectrum after background subtraction. For the true $2\nu 2\beta$ decay distribution, such a Kurie plot should be a straight line $K(\varepsilon) \sim (Q_{2\beta} - \varepsilon)$. The obtained experimental Kurie plot is depicted in the inset of Fig. 9, from which one can see that in the energy region 0.9–2.5 MeV it is indeed well fitted by the straight line with $Q_{2\beta} = 2808(43)$ keV (the table value is $Q_{2\beta} = 2805(4) \text{ keV } [40]).^4$

It should be stressed that statistics collected in our experiment (9846 events of $2\nu 2\beta$ decay of ¹¹⁶Cd within the energy interval 800–2800 keV) and a signal to background ratio (3:1 for the energy interval 1.2–2.8 MeV and 8:1 for the energy range 1.9–2.2 MeV) are among the highest ones reached up to date in 2β decay experiments [6–8].

Different origins of systematical uncertainties of the measured half-life were taken into account (see Table II). The main ones are the above mentioned half-life changes for the fitting in different energy regions, and possible traces of the β active nuclides ^{234m}Pa and ⁹⁰Y (daughter of ⁹⁰Sr) in the ¹¹⁶CdWO₄ crystals. In fact, both these causes are related to background model description which is a typical problem of data interpretation in low background experiments. From the upper limit on ²²⁶Ra contamination, derived with the help of the time-amplitude analysis of the data, it is obtained that activity of ²³⁸U (and therefore of ^{234m}Pa) in the enriched crystals is less than 0.7 mBq/kg.⁵ To estimate a systematic uncertainty, both β nuclides (^{234m}Pa and ⁹⁰Sr–⁹⁰Y) were included in the fitting procedure, which leads to the stronger bound on their total activity ≤ 0.3 mBq/kg.

The final half-life value is equal to

$$T_{1/2}^{2\nu} = 2.9 \pm 0.06 (\text{stat})_{-0.3}^{+0.4} (\text{syst}) \times 10^{19} \text{ yr.}$$

This value is in agreement with our preliminary result $T_{1/2}^{2\nu} = 2.6_{-0.4}^{+0.7} \times 10^{19} \text{ yr [15]}$, and with those measured earlier in other experiments: $T_{1/2}^{2\nu} = 2.6_{-0.5}^{+0.9} \times 10^{19} \text{ yr [41]}$, $T_{1/2}^{2\nu} = 2.7_{-0.4}^{+0.5} (\text{stat})_{-0.6}^{+0.9} (\text{syst}) \times 10^{19} \text{ yr [24]}$, and $T_{1/2}^{2\nu} = 3.75 \pm 0.35 (\text{stat}) \pm 0.21 (\text{syst}) \times 10^{19} \text{ yr [42]}$.

³The fitting interval has been chosen as a compromise between several contradicting demands: (i) the high statistics accumulated; (ii) the large ratio of the effect to background; (iii) the maximal energy range of the $2\nu 2\beta$ decay spectrum; (iv) the goodness of the fit; (v) the reasonably small uncertainties of fitting parameters, etc. It is remarkable to note that the results of the fit were rather stable for the different energy intervals in the range (800–2800) keV; so, the corresponding values of half-life varied in the range of $(2.6-3.1)\times10^{19}$ yr. Actually, such changes of the half-life value result mainly from the background model uncertainties.

⁴To take into account the energy resolution of the detector, the fitting procedure was repeated by using the convolution of the theoretical $2\nu 2\beta$ distribution $\rho(\varepsilon) = A\varepsilon(\varepsilon^4 + 10\varepsilon^3 + 40\varepsilon^2 + 60\varepsilon + 30)$ $(Q_{2\beta} - \varepsilon)^5$ with the detector resolution function (*A*, which is inverse proportional to $T_{1/2}^{2\nu}$, and $Q_{2\beta}$ were taken as free parameters). The fit in the energy region 1.2–2.8 MeV yields similar $Q_{2\beta}$ and half-life values: $Q_{2\beta} = 2748(42)$ keV; $T_{1/2} = 2.9(1) \times 10^{19}$ yr.

⁵This estimation was derived from the limit on the ²²⁶Ra activity ($\leq 4 \ \mu$ Bq/kg), conservatively supposing that all ²²⁶Ra nuclei were produced from ²³⁸U contamination in the crystals during ≈ 13 yr after their growth. An analysis of α spectra [33] gives estimation of ≤ 0.6 mBq/kg for the total activity of ²³⁸U and ²³⁴U.



FIG. 8. (Color online) Simulated response functions of the ¹¹⁶CdWO₄ crystal scintillators for the $2\nu 2\beta$ (a) and $0\nu 2\beta$ (b) decay of ¹¹⁶Cd to excited levels of ¹¹⁶Sn.

Besides, we have also searched for the possible $2\nu 2\beta$ decay of ¹¹⁶Cd to excited levels of ¹¹⁶Sn [see Fig. 8(a)]: 2⁺ with $E_{lev} = 1294$ keV, 0_1^+ with $E_{lev} = 1757$ keV, and 0_2^+ with $E_{lev} = 2027$ keV. However, the probabilities of such 2β transitions should be strongly suppressed due to reduced energy releases (for example, the theoretical predictions for their half-lives are in the range of $10^{22}-10^{24}$ yr [8]). Because of the absence in the experimental data of any indications on these processes, we only set the bounds on their half-lives with the help of the formula: $\lim T_{1/2} = \ln 2Nt \eta / \lim S$, where N is the number of ¹¹⁶Cd nuclei, t the measuring time, η the total detection efficiency, and lim S the number of events of the effect searched for, which can be excluded with a given confidence level. The value of the detection efficiency was calculated by using the GEANT3.21 and DECAY4 codes as $\eta_{mc}(2^+) = 0.18, \ \eta_{mc}(0^+_1) = 0.09, \ \text{and} \ \eta_{mc}(0^+_2) = 0.06.$ Taking into account the efficiency of the pulse-shape analysis $\eta_{psa} = 0.97$, this gives the total efficiencies $\eta(2^+) = 0.18$, $\eta(0_1^+)=0.09$, and $\eta(0_2^+)=0.06$. To estimate the value of limS, the fit described above was repeated in the energy interval 1.7-2.7 MeV by adding the simulated response functions for the effect searched for. It yields S = -33 ± 108 counts (2⁺), $S = -53 \pm 59$ counts (0⁺₁), and S = -3 ± 47 counts (0_2^+) , which corresponds, in accordance with the Feldman-Cousins procedure [43] recommended by the Particle Data Group [44], to the restrictions on the half-lives of $2\nu 2\beta$ decay of $11\overline{6}$ Cd to excited levels of $2\nu 2\beta$ decay of ¹¹⁶Cd to excited levels of ¹¹⁶Sn at 90% (68%) C.L.:

$$T_{1/2}^{2\nu}(g.s.\rightarrow 2^+) \ge 0.6(1.1) \times 10^{21}$$
 yr,



FIG. 9. (Color online) The part of $\gamma(\beta)$ spectrum measured with ¹¹⁶CdWO₄ detectors during 12 649 h, which was used for the determination of the half-life of $2\nu 2\beta$ decay of ¹¹⁶Cd. Also shown are the most important model components: (a) the $2\nu 2\beta$ spectrum of ¹¹⁶Cd; (b) external γ background caused by ⁴⁰K, ²³²Th, and ²³⁸U contamination of the PMTs; ⁴⁰K contamination of the nonenriched (c) and enriched (d) CdWO₄ scintillators. Solid line represents the fit of the data in the 860–2700 keV energy interval. Inset: The $2\nu 2\beta$ decay Kurie plot and its fit by a straight line in the 900–2500-keV-energy region.

$$T_{1/2}^{2\nu}(g.s.\rightarrow 0_1^+) \ge 0.8(2.2) \times 10^{21} \text{ yr},$$

 $T_{1/2}^{2\nu}(g.s.\rightarrow 0_2^+) \ge 0.4(0.6) \times 10^{21} \text{ yr}.$

C. Neutrinoless double β decay of ¹¹⁶Cd

The part of the spectrum of the ¹¹⁶CdWO₄ crystals measured during 14 183 h in anticoincidence with the shielding detectors and after the time-amplitude and pulse-shape selection is shown in Fig. 10. The exposure corresponds to 7.41 $\times 10^{23}$ (nuclei of ¹¹⁶Cd) \times yr. This spectrum includes also data obtained in the first part of the experiment [15]. The energy resolution and the efficiency of the pulse-shape discrimination were calculated for the full exposition, taking into account results of the calibration measurements. For instance, for the total spectrum the energy resolution at 2.8 MeV was 8.9%.

The background rate in the energy interval 2.5–3.2 MeV is 0.037(10) counts/(yrkg keV). The peak of $0\nu 2\beta$ decay is absent, thus we obtain a lower limit on the half-life. The efficiency to detect this peak in crystals was calculated by the Monte Carlo method (with the help of GEANT3.21 and DECAY4 codes) as $\eta_{mc} = 0.83$. Again by taking into account the efficiency of the pulse-shape analysis $\eta_{psa} = 0.96$, it yields a total efficiency $\eta = 0.80$. To estimate lim *S*, the part of the spectrum in the 2.0–3.6 MeV energy interval was fitted by the sum of the simulated $0\nu 2\beta$ peak and three background functions: $2\nu 2\beta$ decay (contribution to the experimental spectrum is $\approx 83\%$), γ rays from PMTs ($\approx 14\%$), and background from the intrinsic chain ²²⁸Th ($\approx 3\%$). For the fit



FIG. 10. (Color online) The high energy part of the experimental spectrum of the ¹¹⁶CdWO₄ detectors measured during 14 183 h (histogram) together with the fit from $2\nu 2\beta$ contribution $(T_{1/2}^{2\nu} = 2.9 \times 10^{19} \text{ yr})$. The smooth curves $0\nu M1$, $0\nu M2$, and $0\nu bM$ are excluded with 90% C.L. distributions of $0\nu 2\beta$ decay of ¹¹⁶Cd with emission of one, two, and bulk Majorons, respectively: $T_{1/2}^{0\nu M1} = 8.0 \times 10^{21} \text{ yr}, \quad T_{1/2}^{0\nu M2} = 8.0 \times 10^{20} \text{ yr}, \text{ and } T_{1/2}^{0\nu bM} = 1.7 \times 10^{21} \text{ yr}$. In the inset the expected peak from $0\nu 2\beta$ decay with $T_{1/2}^{0\nu} = 2 \times 10^{22} \text{ yr}$ is shown.

these background activities were taken as free parameters and varied within their errors. This maximum likelihood fit $(\chi^2/\text{ndf}=37/33=1.1)$ gives the area of the $0\nu 2\beta$ peak as $S=0.3\pm1.3$ counts, which corresponds to $\lim S=2.4$ (1.6) counts with 90% (68%) C.L.,⁶ and to a half-life limit for the $0\nu 2\beta$ decay of ¹¹⁶Cd:

$$T_{1/2}^{0\nu} \ge 1.7(2.6) \times 10^{23}$$
 yr at 90% (68%) C.L.

Excited levels of ¹¹⁶Sn with $E_{lev} \leq Q_{2\beta}$ can be also populated in the $0\nu 2\beta$ decay of ¹¹⁶Cd [the corresponding response functions are shown in Fig. 8(b)]. The full absorption of all emitted particles should result in a peak with $E = Q_{2\beta}$. The full peak efficiencies calculated with the help of the GEANT3.21 and DECAY4 codes for the $0\nu 2\beta$ decay to the first, second, and third excited levels of ¹¹⁶Sn are $\eta_{mc}(2^+) = 0.14$, $\eta_{mc}(0^+_1) = 0.07$, and $\eta_{mc}(0^+_2) = 0.03$. These numbers result in the following restrictions on half-life of ¹¹⁶Cd $0\nu 2\beta$ decay to excited levels of ¹¹⁶Sn at 90% (68%) C.L.:

$$T_{1/2}^{0\nu}(g.s.\rightarrow 2^{+}) \ge 2.9(4.3) \times 10^{22} \text{ yr},$$

$$T_{1/2}^{0\nu}(g.s.\rightarrow 0^{+}_{1}) \ge 1.4(2.2) \times 10^{22} \text{ yr},$$

$$T_{1/2}^{0\nu}(g.s.\rightarrow 0^{+}_{2}) \ge 0.6(0.9) \times 10^{22} \text{ yr}.$$

To obtain the half-life limits for the $0\nu 2\beta$ decay with emission of one, two, and bulk [45] Majoron(s), the measured spectrum was fitted in the energy region 1.6–2.8 MeV by using the same model of background as for the $0\nu 2\beta$ decay fitting procedure. As a result, the number of events under a theoretical 0ν M1 curve was determined as -37 ± 56 , giving no statistical evidence for the effect. Again, following the Particle Data Group (PDG) recommendation, it leads to an upper limit of 59 (25) events at 90% (68%) C.L., which together with an efficiency value $\eta_{mc} = 0.905$ corresponds to a half-life limit

$$T_{1/2}^{0\nu M1} \ge 0.8(1.8) \times 10^{22}$$
 yr at 90% (68%) C.L.

A similar procedure for the $0\nu 2\beta$ decay with two and bulk Majorons emission gives the following results at 90% (68%) C.L.:

$$T_{1/2}^{0\nu M2} \ge 0.8(1.4) \times 10^{21} \text{ yr},$$

$$T_{1/2}^{0\nu bM} \ge 1.7(2.3) \times 10^{21} \text{ yr}.$$

Excluded with 90% C.L. distributions of $0\nu M1, 0\nu M2$, and 0ν decay with bulk Majoron emission are shown in Fig. 10.

D. Limits on 2β decay processes in ¹⁰⁶Cd, ¹⁰⁸Cd, ¹¹⁴Cd, ¹⁸⁰W, and ¹⁸⁶W

The ¹¹⁶CdWO₄ crystals contain not only ¹¹⁶Cd nuclei but several other potentially 2 β decaying isotopes: ¹⁰⁶Cd with abundance δ =0.16% [25] and $Q_{\beta\beta}$ =2771 keV [40], ¹⁰⁸Cd (δ =0.11% [25], $Q_{\beta\beta}$ =269 keV), ¹¹⁴Cd (δ =6.5% [25], $Q_{\beta\beta}$ =537 keV), ¹⁸⁰W (δ =0.12% [46], $Q_{\beta\beta}$ =146 keV), and ¹⁸⁶W (δ =28.4% [46], $Q_{\beta\beta}$ =488 keV). It allows us to establish bounds on 2 β decay processes in these nuclides.

The spectrum of Fig. 5 was used to search for the $0\nu 2\beta$ decay of ¹¹⁴Cd (g.s.-g.s. transition) and for the $0\nu 2\beta$ decay of ¹⁸⁶W to the ground and to the first excited (2⁺) levels of ¹⁸⁶Os. In the energy range of interest (440–600 keV), where the background rate is equal to 0.295(3) counts/(day keV kg), there is no indication for the positive $0\nu 2\beta$ decay peak of ¹⁸⁶W searched for. Hence, we can only set a limit on its probability. Taking into account the registration efficiency of the ¹¹⁶CdWO₄ scintillators for this process (η_{mc} =0.99), and the efficiency of the PSA (η_{psa} =0.95), the total detection efficiency is η =0.94.

The value of lim *S* was determined by using the standard χ^2 procedure, where the experimental spectrum in the (380–1200)-keV-energy interval was fitted by the sum of the $0\nu 2\beta$ decay peak being sought and the background components determined above (^{113m}Cd, ¹³⁷Cs, exponential function representing external γ rays, and $2\nu 2\beta$ decay of ¹¹⁶Cd). The fit (χ^2 /ndf=38/36=1.1) yields the peak area (-21±95)

⁶As it was noted earlier (see Sec. II A), the energy resolution of the spectrometer was carefully tested during the experiment. Nevertheless, to check the possible influence of energy resolution on the limS estimation, the fit has been repeated for the different FWHM values (8%, 9%, 10%, and 11% at 2.8 MeV), which were taken into account in all the background models. As it was found, the variation of the limS does not exceed $\pm 15\%$. In addition, the fit has been also performed for the different energy intervals in the energy region 1900–3800 keV, and resulting changes of the limS were within $\pm 25\%$ of the central value.

counts, i.e., no evidence for the effect. Using the PDG recommendation, one can get $\lim S = 136$ (75) counts at 90% (68%) C.L. Taking into account these values, the efficiency $\eta = 0.94$, and the number of ¹⁸⁶W nuclei (1.56×10^{23}), we derive the following half-life limit on the $0\nu 2\beta$ decay of ¹⁸⁶W to the ground level of ¹⁸⁶Os:

$$T_{1/2}^{0\nu} \ge 1.1(2.1) \times 10^{21}$$
 yr at 90% (68%) C.L.

In the case of ¹⁸⁶W neutrinoless 2β decay to the first excited (2⁺) level of ¹⁸⁶Os, γ quanta with an energy of 137 keV (deexcitation of the 2⁺ level of ¹⁸⁶Os) will be emitted. Due to practically full absorption of these γ quanta in the ¹¹⁶CdWO₄ crystals, the expected response function does not differ from that for transition to ground state. The total efficiency is equal to η =0.92, and leads to the half-life limit

$$T_{1/2}^{0\nu}(\text{g.s.}\rightarrow 2^+) \ge 1.1(2.0) \times 10^{21} \text{ yr at } 90\% (68\%) \text{ C.L.}$$

For the $0\nu 2\beta$ decay of ¹⁸⁶W with an emission of Majoron, the fit of the spectrum gives

$$T_{1/2}^{0\nu M1} \ge 1.2(1.4) \times 10^{20}$$
 yr at 90% (68%) C.L.

To estimate the lower limit for the $2\nu 2\beta$ decay of ¹⁸⁶W, we have considered the background spectrum accumulated during 692 h with the low energy threshold (Fig. 6). Because practically 100% of the β particles from the expected $2\nu 2\beta$ decay are absorbed in the crystals, the total efficiency is determined by the PSA ($\eta = \eta_{psa} = 0.98$). A simple model (which includes the $2\nu 2\beta$ spectrum of ¹⁸⁶W, the β spectrum of ¹¹³Cd, and an exponential function) was used to describe the experimental data in the energy interval 130–450 keV. The fit ($\chi^2/ndf = 42/29 = 1.5$) gives 489 ± 1119 events for the effect searched for. It yields 2324 (1608) counts excluded at 90% (68%) C.L., and the half-life limit for the $2\nu 2\beta$ decay of ¹⁸⁶W:

 $T_{1/2}^{2\nu} \ge 3.7(5.3) \times 10^{18}$ yr at 90% (68%) C.L.

The $2\nu 2\beta$ decay distribution of ¹⁸⁶W excluded at 90% C.L. is depicted in Fig. 6.

The same method gives the bound for $2\nu 2\beta$ transition to the first (2⁺) excited level of ¹⁸⁶Os:

$$T_{1/2}^{2\nu}(g.s. \rightarrow 2^+) \ge 1.0(1.3) \times 10^{19} \text{ yr at } 90\% (68\%) \text{ C.L.}$$

Similar procedures were used to search for 2β decay processes in ¹¹⁴Cd and the obtained bounds are presented in Table III.

In accordance with the level scheme of the $^{180}W_{-}^{180}Ta_{-}^{180}Hf$ triplet [36], the double electron capture (2ε) of ^{180}W ($Q_{2\varepsilon} = 146$ keV) is allowed. In the case of 2ν double electron capture from the *K* shell $(2\nu 2K)$, the total energy released in a detector is equal to $2E_K$ (where $E_K = 65.4$ keV is the binding energy of electrons on the *K* shell of hafnium atom), while the rest of the energy ($Q_{2\varepsilon} - 2E_K \approx 15$ keV) is carried away by neutrinos. For the neutrinoless double electron capture $(0\nu 2\varepsilon)$, all available energy (trans-

ferred to X rays, Auger electrons, γ quanta, or conversion electrons) will result in a peak at $Q_{2\epsilon} = 146$ keV value.

To set the limits on the $0\nu 2\varepsilon$ process in ¹⁸⁰W, the background spectrum measured with the ¹¹⁶CdWO₄ detector during 692 h (Fig. 6) was fitted in the 90–240-keV energy interval, which gives 91±177 counts for the peak searched for $(\chi^2/ndf=18/14=1.3)$. These numbers lead to an upper limit of 381 (268) counts at 90% (68%) C.L. Taking into account the total efficiency $\eta = \eta_{psa} = 0.98$ and the number of ¹⁸⁰W nuclei (6.57×10^{20}) , one can calculate the half-life limit

$$T_{1/2}^{0\nu 2\varepsilon} \ge 0.9 \ (1.3) \times 10^{17} \text{ yr at } 90\% \ (68\%) \text{ C.L.}$$

The same method gives restriction for the $2\nu 2K$ process in ¹⁸⁰W:

$$T_{1/2}^{2\nu 2K} \ge 0.7(0.8) \times 10^{17}$$
 yr at 90% (68%) C.L.

The peaks of the $0\nu 2\varepsilon$ and $2\nu 2K$ captures in ¹⁸⁰W excluded at 90% C.L. are shown in the inset of Fig. 6.

Similarly, by using the described procedures, the bounds on neutrinoless double electron capture in ¹⁰⁸Cd were extracted from our experimental data. Because of absence of the peak at the transition energy ($Q_{\beta\beta}=269 \text{ keV}$), the fit of the spectrum of Fig. 6 yields the half-life limit for the $0\nu 2\varepsilon$ capture in ¹⁰⁸Cd: $T_{1/2}^{0\nu 2\varepsilon} \ge 1.5(2.5) \times 10^{17}$ yr at 90% (68%) C.L.

To search for the $2\nu 2K$ capture in ¹⁰⁶Cd and ¹⁰⁸Cd with an energy release $2E_K \approx 49$ keV (where $E_K = 24.4$ keV is the binding energy of electrons on the *K* shell of palladium atom), a detector with a low energy threshold is needed. With this aim the results of dedicated measurements (433 h) with the nonenriched CdWO₄ crystal (454 g) were used [35]. The energy resolution of this detector at 60 keV (γ rays of ²⁴¹Am) was FWHM = 25 keV, while the energy threshold was ≈ 40 keV. This crystal contains 9.5×10^{21} and 6.8 $\times 10^{21}$ nuclei of ¹⁰⁶Cd and ¹⁰⁸Cd, respectively. The measured spectrum [35] was fitted by the sum of the expected peak at the energy of 49 keV and a background model (β spectrum of ¹¹³Cd). It gives the following half-life limits on $2\nu 2\varepsilon$ capture: $T_{1/2}^{2\nu 2K} \ge 5.8$ (9.5) $\times 10^{17}$ yr at 90% (68%) C.L. for ¹⁰⁶Cd, and $T_{1/2}^{2\nu 2K} \ge 4.1$ (6.7) $\times 10^{17}$ yr at 90% (68%) C.L. for ¹⁰⁸Cd.

As it is visible from the level scheme of the ¹⁰⁶Cd-¹⁰⁶Ag-¹⁰⁶Pd triplet [Fig. 11(a)], besides the double electron capture (2 ε) also the double positron decay ($\beta^+\beta^+$), and the electron capture and positron decay ($\varepsilon\beta^+$) are allowed for ¹⁰⁶Cd (both to the ground state and to excited levels of ¹⁰⁶Pd). The Monte Carlo simulated response functions of the ¹¹⁶CdWO₄ detector to the 0 ν modes of these processes are presented in Fig. 11(b). One can see from this figure that each of the mentioned processes will result in the full absorption peak at the energy 2771 keV with the width FWHM = 216 keV. The values of the efficiency to detect such a peak were calculated as follows: η_{mc} (0 $\nu \varepsilon\beta^+$, g.s. \rightarrow g.s.) = 0.015; η_{mc} (0 $\nu \varepsilon\beta^+$, g.s. \rightarrow g.s.) = 0.128; η_{mc} (0 $\nu \varepsilon\beta^+$, g.s. \rightarrow g.s.)=0.027; η_{mc} (0 $\nu \beta^+\beta^+$, g.s. \rightarrow 2⁺, 512 keV)=0.059; η_{mc} (0 $\nu \beta^+\beta^+$, g.s. \rightarrow 2⁺, 512 keV)

Nuclide	lide Decay mode, Transition (level energy)			$T_{1/2}$ limit or value (yr) 90% (68)% C.L.	
¹⁰⁶ Cd	2ε	0ν	g.sg.s.	$\geq 0.8(1.7) \times 10^{19}$	
	$arepsiloneta^+$	0ν	g.sg.s.	$\geq 0.7(1.6) \times 10^{20}$	
		0ν	$g.s2^+_1$ (511.9 keV)	$\geq 3.1(7.2) \times 10^{19}$	
		0ν	$g.s2^+_2$ (1128.0 keV)	$\geq 1.4(3.3) \times 10^{19}$	
		0ν	g.s 0_1^+ (1133.8 keV)	$\geq 1.4(3.2) \times 10^{19}$	
	$2\beta^+$	0ν	g.sg.s.	$\geq 1.4(3.3) \times 10^{19}$	
		0ν	$g.s2^+_1$ (511.9 keV)	$\geq 0.6(1.5) \times 10^{19}$	
	2K	2ν	g.sg.s.	\geq 5.8(9.5)×10 ¹⁷	
	$arepsiloneta^+$	2ν	g.sg.s.	$\geq 1.2(2.0) \times 10^{18}$	
	$2\beta^+$	2ν	g.sg.s.	\geq 5.0(8.2)×10 ¹⁸	
¹⁰⁸ Cd	2ε	0ν	g.sg.s.	$\geq 1.5(2.5) \times 10^{17}$	
	2K	2ν	g.sg.s.	$\geq 4.1(6.7) \times 10^{17}$	
¹¹⁴ Cd	$2\beta^{-}$	0ν	g.sg.s.	$\geq 2.5(4.1) \times 10^{20}$	
	$2\beta^{-}$	2ν	g.sg.s.	$\geq 6.0(9.3) \times 10^{17}$	
¹¹⁶ Cd	$2\beta^{-}$	0ν	g.sg.s.	$\geq 1.7(2.6) \times 10^{23}$	
		0ν	g.s2 ⁺ (1293.5 keV)	$\geq 2.9(4.3) \times 10^{22}$	
		0ν	$g.s0^+_1$ (1756.8 keV)	$\geq 1.4(2.2) \times 10^{22}$	
		0ν	$g.s0^+_2$ (2027.3 keV)	$\geq 0.6(0.9) \times 10^{22}$	
		$0 \nu M 1$	g.sg.s.	$\geq 0.8(1.8) \times 10^{22}$	
		$0 \nu M 2$	g.sg.s.	$\geq 0.8(1.4) \times 10^{21}$	
		$0 \nu b M$	g.sg.s.	$\geq 1.7(2.3) \times 10^{21}$	
	$2\beta^{-}$	2ν	g.sg.s.	$=2.9^{+0.4}_{-0.3}\times10^{19}$	
		2ν	g.s2 ⁺ (1293.5 keV)	$\geq 0.6(1.1) \times 10^{21}$	
		2ν	g.s 0_1^+ (1756.8 keV)	$\geq 0.8(2.2) \times 10^{21}$	
		2ν	$g.s0^+_2$ (2027.3 keV)	$\geq 0.4(0.6) \times 10^{21}$	
^{180}W	2ε	0ν	g.sg.s.	$\geq 0.9(1.3) \times 10^{17}$	
	2K	2ν	g.sg.s.	$\geq 0.7(0.8) \times 10^{17}$	
^{186}W	$2\beta^{-}$	0ν	g.sg.s.	$\geq 1.1(2.1) \times 10^{21}$	
		0ν	g.s2 ⁺ (137.2 keV)	$\geq 1.1(2.0) \times 10^{21}$	
		$0 \nu M 1$	g.sg.s.	$\geq 1.2 (1.4) \times 10^{20}$	
	$2\beta^{-}$	2ν	g.sg.s.	$\geq 3.7(5.3) \times 10^{18}$	
		2ν	g.s2 ⁺ (137.2 keV)	$\geq 1.0(1.3) \times 10^{19}$	

TABLE III. Total list of the results obtained on the 2β decay processes in Cd and W nuclides.

= 0.012; etc. The fit of the energy spectrum of Fig. 10 in the energy interval 2.2–3.4 MeV gives the area of the peak searched for as $S = -1.0 \pm 1.6$ counts. The latter leads, for example, to the half-life limit on the $0\nu 2\varepsilon$ capture in ¹⁰⁶Cd: $T_{1/2}^{0\nu 2\varepsilon}(\text{g.s.} \rightarrow \text{g.s.}) \ge 0.8(1.7) \times 10^{19}$ yr at 90% (68%) C.L. In the same way, restrictions on the other 0ν and 2ν double β decays in ¹⁰⁶Cd were derived and they are listed in Table III.

IV. DISCUSSION AND CONCLUSIONS

All half-life limits on 2β decay processes obtained in the present experiment with the help of the low background ¹¹⁶CdWO₄ scintillators are summarized in Table III. It should be stressed that most of the bounds for ¹⁰⁶Cd, ¹⁰⁸Cd, ¹¹⁴Cd, ¹¹⁶Cd, ¹⁸⁰W, and ¹⁸⁶W are higher than the previous results or have been established for the first time. For example, the limit $T_{1/2}^{0\nu} \ge 10^{21}$ yr on the $0\nu 2\beta$ decay of ¹⁸⁶W is nearly one order of magnitude higher than the previous one [25], while the bounds for the 0ν decay with Majoron emis-

sion and for the 2ν decay to the first (2^+) excited level of ¹⁸⁶Os were set for the first time. Note that up to now the level of sensitivity $T_{1/2}^{0\nu} \ge 10^{21}$ yr was reached only for ten nuclides [8]. Nevertheless, the obtained results are still far from the theoretical predictions, which, e.g., for the $0\nu 2\beta$ decay of ¹⁸⁶W are in the range of 6×10^{24} yr [47]–5 $\times 10^{25}$ yr [48] (for $m_{\nu}=1$ eV), thus further efforts in this direction would be needed.

Besides, in the course of the present experiment two important by-products were obtained: (i) the half-life $(T_{1/2} = 7.7^{+0.3}_{-0.3} \times 10^{15} \text{ yr})$ and the spectrum shape of the fourth-forbidden β decay of ¹¹³Cd were measured [35]; (ii) indication for the α decay of ¹⁸⁰W with a half-life $T^{\alpha}_{1/2} = 1.1^{+0.9}_{-0.5} \times 10^{18} \text{ yr}$ has been observed for the first time, and new $T_{1/2}$ bounds were set for α decay of ¹⁸²W, ¹⁸³W, ¹⁸⁴W, and ¹⁸⁶W at the level of 10^{20} yr [33].

As regarding the main results of the present experiment on the 2β decay of ¹¹⁶Cd, note that the refined half-life value of the two-neutrino 2β decay of ¹¹⁶Cd is measured as



FIG. 11. (a) (Color online) The level scheme of the $^{106}\text{Cd}\text{-}^{106}\text{Ag}\text{-}^{106}\text{Pd}$ triplet. (b) Simulated response functions of the $^{116}\text{CdWO}_4$ detector to different $0\,\nu$ modes of the $2\,\beta$ decay processes in ^{106}Cd .

 $T_{1/2}^{2\nu} = 2.9_{-0.3}^{+0.4} \times 10^{19}$ yr. The experimental $2\nu 2\beta$ Kurie plot is well described by a straight line, and the derived $Q_{\beta\beta}$ value (2808±43 keV) is in accordance with the table value 2805(4) keV.

It should be noted that all half-life limits obtained here for ¹¹⁶Cd are the most stringent for that nucleus, as for example, the bound on half-life of the $0\nu 2\beta$ decay of ¹¹⁶Cd (g.s. \rightarrow g.s.):

$$T_{1/2}^{0\nu} \ge 1.7(2.6) \times 10^{23}$$
 yr at 90% (68%) C.L.

Using this bound and calculations [47], one can derive restrictions on the Majorana neutrino mass and right-handed admixtures in the weak interaction: $m_{\nu} \leq 1.9 \text{ eV}$, $\eta \leq 2.5 \times 10^{-8}$, $\lambda \leq 2.2 \times 10^{-6}$ at 90% C.L. Neglecting right-handed contribution we get $m_{\nu} \leq 1.7$ (1.4) eV at 90% (68%) C.L., and on the basis of [42] the limit is $m_{\nu} \leq 1.5$ (1.2) eV. These results together with the best $T_{1/2}^{0\nu}$ limits obtained in the most sensitive direct experiments (and the corresponding restrictions on the Majorana neutrino mass) are given in Table IV. The m_{ν} constraints are determined on the basis of the calculations of Ref. [47], which were chosen because of the extensive list of 2β candidate nuclei calculated in this work, which allows one to compare the sensitivity of different experiments to the m_{ν} bound within the same scale.

It is obvious from Table IV that our experimental result on ¹¹⁶Cd is one of the best after those based on ⁷⁶Ge studies and offers the restriction on the neutrino mass at the level of ≈ 1.5 eV similar to those of experiments with ¹³⁰Te and ¹³⁶Xe. In accordance with Ref. [50] the value of the R-parity violating parameter of minimal SUSY standard model is restricted by our $T_{1/2}^{0\nu}$ limit to $\varepsilon \le 7.0(6.3) \times 10^{-4}$ at 90% (68%) C.L. (calculations [51] give more stringent restrictions: ε $\leq 2.7(2.4) \times 10^{-4}$). Moreover, using our bound on the $0\nu 2\beta$ decay with one Majoron emission: $T_{1/2}^{0\nu} \ge 0.8(1.8) \times 10^{22}$ yr at 90% (68%) C.L. and calculations [52] the effective Majoronneutrino coupling constant can be restricted to g_M $\leq 8.1(5.4) \times 10^{-5}$, and on the basis of calculation [42] to $g_M \leq 4.6(3.1) \times 10^{-5}$, which are among the strongest constraints obtained up to date in the direct 2β decay experiments with 76 Ge, 82 Se, 100 Mo, 130 Te, and 136 Xe [8].

We consider the Solotvina experiment on the 2β decay of ¹¹⁶Cd as a pilot study for the future large scale project CAMEO [53], which intends to operate ≈ 100 kg of enriched ¹¹⁶CdWO₄ crystals allocated in the liquid scintillator of the BOREXINO Counting Test Facility. Results of our measurements with ¹¹⁶Cd and Monte Carlo simulations evidently show that sensitivity (in terms of the half-life limit for the $0\nu 2\beta$ decay) of the CAMEO experiment with 100 kg of enriched ¹¹⁶CdWO₄ crystals is of the order of 10^{26} yr [53]. The last value corresponds to a limit on the neutrino mass $m_{\nu} \leq 0.06$ eV, which would be of great interest for the modern physics.

Nuclide	Experimental limit $T_{1/2}^{0\nu}$ (yr)		Reference	Limit on m_{ν} (eV) on the basis of Ref. [47]	
	68% C.L.	90% C.L.		68% C.L.	90% C.L.
⁷⁶ Ge	3.1×10^{25}	$\frac{1.9 \times 10^{25}}{1.6 \times 10^{25}}$	[18] [19]	0.27	0.35 0.38
	4.2×10^{25} a	2.5×10^{25} a	[49]	0.24	0.31
¹¹⁶ Cd ¹³⁰ Te ¹³⁶ Xe	2.6×10 ²³	$ \begin{array}{r} 1.7 \times 10^{23} \\ 2.1 \times 10^{23} \\ 4.4 \times 10^{23} \end{array} $	Present work [16] [17]	1.4	1.7 1.5 2.2

TABLE IV. The best reported $T_{1/2}^{0\nu}$ and m_{ν} limits from direct 2β decay experiments.

^aResults were established [49] by analyzing the cumulative datasets of the Heidelberg-Moscow [18] and IGEX [19] experiments.

ACKNOWLEDGMENTS

The authors express their gratitude to V.N. Kuts, V.V. Muzalevsky and S.S. Nagorny, who have contributed to the development, preparation, and fulfillment of the Solotvina

- Y. Fukuda *et al.*, Super-Kamiokande Collaboration, Phys. Rev. Lett. **81**, 1562 (1998); **82**, 1810 (1999); **82**, 2430 (1999); **86**, 5651 (2001).
- [2] Q.R. Ahmad *et al.*, SNO Collaboration, Phys. Rev. Lett. 87, 071301 (2001); 89, 011301 (2002); 89, 011302 (2002).
- [3] K. Eguchi *et al.*, KamLAND Collaboration, Phys. Rev. Lett. 90, 021802 (2003).
- [4] M.H. Ahn et al., Phys. Rev. Lett. 90, 041801 (2003).
- [5] J.D. Vergados, Phys. Rep. **361**, 1 (2002).
- [6] Yu.G. Zdesenko, Rev. Mod. Phys. 74, 663 (2002).
- [7] S.R. Elliott and P. Vogel, Annu. Rev. Nucl. Part. Sci. 52, 115 (2002).
- [8] V.I. Tretyak and Yu.G. Zdesenko, At. Data Nucl. Data Tables 80, 83 (2002).
- [9] R.K. Bardin *et al.*, Nucl. Phys. A158, 337 (1970); V.B. Brudanin *et al.*, Phys. Lett. B 495, 63 (2000).
- [10] A.A. Klimenko *et al.*, Nucl. Instrum. Methods Phys. Res. B
 17, 445 (1986); A. De Silva *et al.*, Phys. Rev. C 56, 2451 (1997).
- [11] F.A. Danevich et al., Nucl. Phys. A694, 375 (2001).
- [12] F.A. Danevich et al., Nucl. Phys. A717, 129 (2003).
- [13] S.R. Elliott et al., Phys. Rev. C 46, 1535 (1992).
- [14] H. Ejiri et al., Phys. Rev. C 63, 065501 (2001).
- [15] F.A. Danevich et al., Phys. Rev. C 62, 045501 (2000).
- [16] C. Arnaboldi et al., Phys. Lett. B 557, 167 (2003).
- [17] R. Luescher et al., Phys. Lett. B 434, 407 (1998).
- [18] H.V. Klapdor-Kleingrothaus *et al.*, Eur. Phys. J. A **12**, 147 (2001).
- [19] C.E. Aalseth *et al.*, Phys. Rev. C 59, 2108 (1999); Phys. Rev. D 65, 092007 (2002).
- [20] Yu. G. Zdesenko et al., in Proceedings of the Second International Symposium on Underground Physics, Baksan Valley, 1987, edited by G.V. Domogatsky (Nauka, Moscow, 1988), p. 291.
- [21] F.A. Danevich *et al.*, Pis'ma Zh. Eksp. Teor. Fiz. **49**, 417 (1989) [JETP Lett. **49**, 476 (1989)].
- [22] Yu.G. Zdesenko, J. Phys. G 17, s243 (1991).
- [23] F. A. Danevich et al., in Proceedings of the Third International Symposium on Weak and Electromagnetic Interaction in Nuclei (WEIN-92), Dubna, Russia, 1992, edited by Ts.D. Vylov (World Scientific, Singapore, 1993), p. 575.
- [24] F.A. Danevich et al., Phys. Lett. B 344, 72 (1995).

experiment at its different stages. We would also like to thank the staff of the Solotvina Underground Laboratory, in particular, M.S. Sheichuk and D.Yu. Sedlak for the technical support of the measurements. One of us (F.A.D.) wishes to thank the INFN Sezione di Firenze for support during his several stays in Firenze.

- [25] A.Sh. Georgadze *et al.*, Yad. Fiz. **58**, 1170 (1995) [Phys. At. Nucl. **58**, 1093 (1995)].
- [26] F.A. Danevich *et al.*, Nucl. Phys. B (Proc. Suppl.) 48A, 232 (1996).
- [27] F.A. Danevich et al., Nucl. Phys. A643, 317 (1998).
- [28] F.A. Danevich *et al.*, Nucl. Phys. B (Proc. Suppl.) **70A**, 246 (1999).
- [29] P.G. Bizzeti et al., Nucl. Phys. B (Proc. Suppl.) 110A, 389 (2002).
- [30] A.Sh. Georgadze *et al.*, Prib. Tekh. Eksp. **3**, 48 (1996) [Instrum. Exp. Tech. **39**, 191 (1996)].
- [31] S.Ph. Burachas *et al.*, Nucl. Instrum. Methods Phys. Res. A 369, 164 (1996).
- [32] T. Fazzini *et al.*, Nucl. Instrum. Methods Phys. Res. A **410**, 213 (1998).
- [33] F.A. Danevich et al., Phys. Rev. C 67, 014310 (2003).
- [34] E. Gatti and F. De Martini, Nuclear Electronics 2 (IAEA, Vienna, 1962), p. 265.
- [35] F.A. Danevich *et al.*, Yad. Fiz. **59**, 5 (1996) [Phys. At. Nucl. **59**, 1 (1996)].
- [36] *Table of Isotopes*, 8th ed. edited by R. B. Firestone *et al.* (Wiley New York, 1996).
- [37] CERN Program Library Long Write-Up W5013, 1994.
- [38] O.A. Ponkratenko *et al.*, Yad. Fiz. **63**, 1355 (2000) [Phys. At. Nucl. **63**, 1282 (2000)].
- [39] F. A. Danevich et al. (unpublished).
- [40] G. Audi and A.H. Wapstra, Nucl. Phys. A595, 409 (1995).
- [41] H. Ejiri et al., J. Phys. Soc. Jpn. 64, 339 (1995).
- [42] R. Arnold et al., Z. Phys. C 72, 239 (1996).
- [43] G.J. Feldman and R.D. Cousins, Phys. Rev. D 57, 3873 (1998).
- [44] K. Hagiwara et al., Phys. Rev. D 66, 010001 (2002).
- [45] R.N. Mohapatra et al., Phys. Lett. B 491, 143 (2000).
- [46] K.J.R. Rosman and P.D.P. Taylor, Pure Appl. Chem. 70, 217 (1998).
- [47] A. Staudt et al., Europhys. Lett. 13, 31 (1990).
- [48] J.G. Hirsch, O. Castanos, and P.O. Hess, Nucl. Phys. A582, 124 (1995).
- [49] Yu.G. Zdesenko et al., Phys. Lett. B 546, 206 (2002).
- [50] M. Hirsch et al., Phys. Rev. D 53, 1329 (1996).
- [51] A. Faessler et al., Phys. Rev. D 58, 115004 (1998).
- [52] M. Hirsch et al., Phys. Lett. B 372, 8 (1996).
- [53] G. Bellini *et al.*, Phys. Lett. B **493**, 216 (2000); Eur. Phys. J. C **19**, 43 (2001).